



# Cooperative Passivity-Based Control for End-Effector Synchronisation

*Oscar de Groot, Tamás Keviczky, Laurens Valk  
Delft University of Technology*



# Outline

- Introduction
- Passivity
- Cooperative  $r$ -Passivity-Based Control
- Experimental Results
- Conclusions

# Introduction



# Our Objective

*Synchronise end-effectors of mechanical systems in general environments.*

Introduction

Passivity

Cooperative rPBC

Experimental  
Results

Conclusions

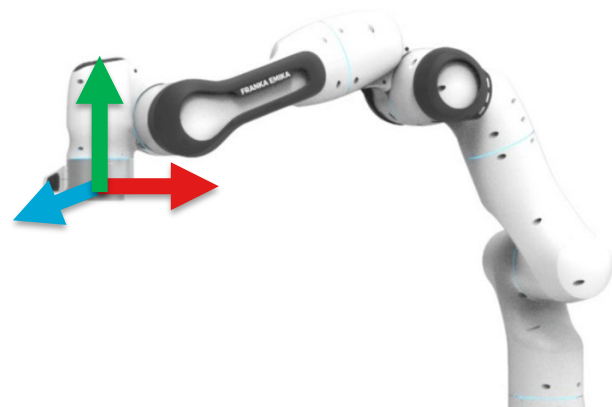
# Our Objective

*Synchronise end-effectors of **mechanical systems** in general environments.*



# Our Objective

Synchronise *end-effectors* of mechanical systems in general environments.



# Possible applications

- Sort and packing problems
- Multi-vehicle package delivery
- Autonomous platoons
- Spacecraft alignment
- ...

Introduction

Passivity

Cooperative rPBC

Experimental  
Results

Conclusions



# Our Objective

*Synchronise end-effectors of mechanical systems in **general environments**.*

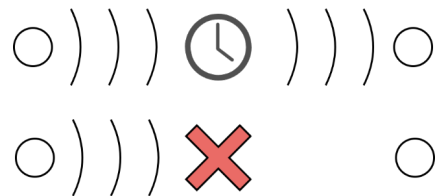
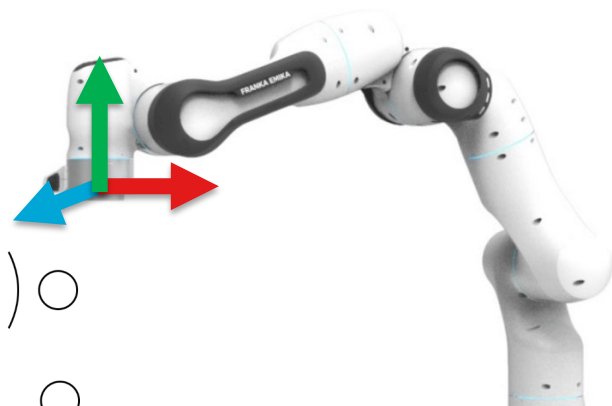
Introduction

Passivity

Cooperative rPBC

Experimental Results

Conclusions

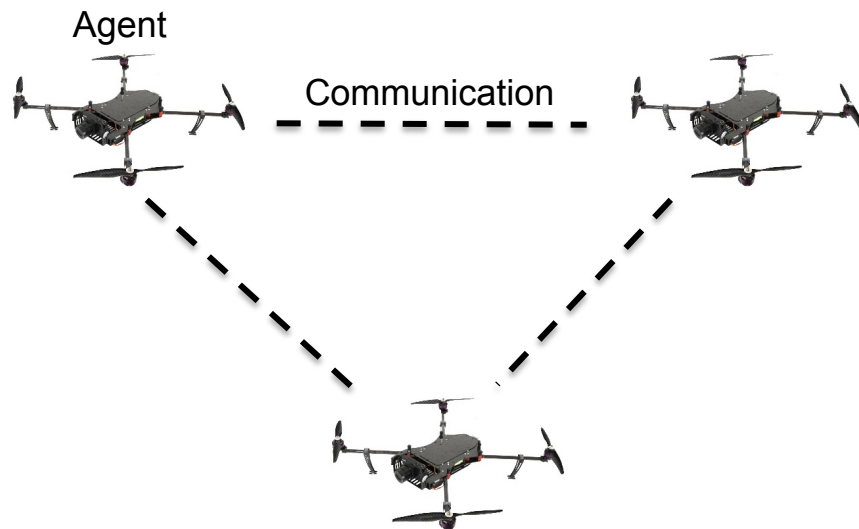






# The approach

## Cooperative Passivity-Based Control



Introduction

Passivity

Cooperative rPBC

Experimental  
Results

Conclusions

# The approach

## Cooperative Passivity-Based Control

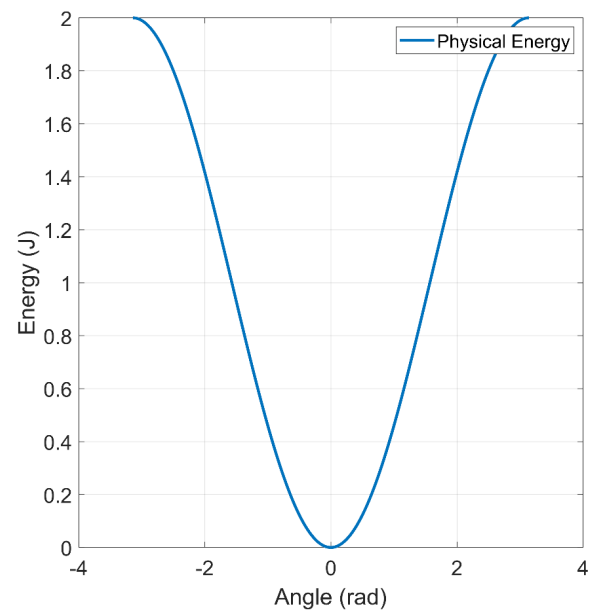
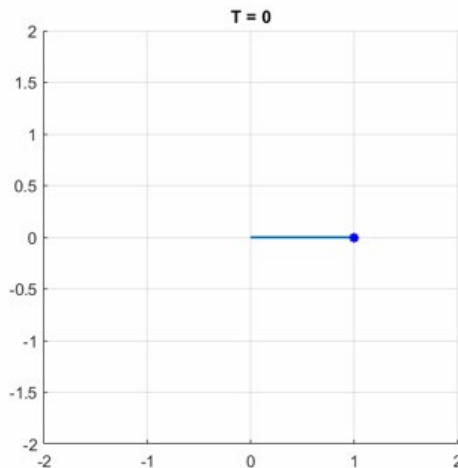
Problem Definition

IDA-PBC

Network Scheme

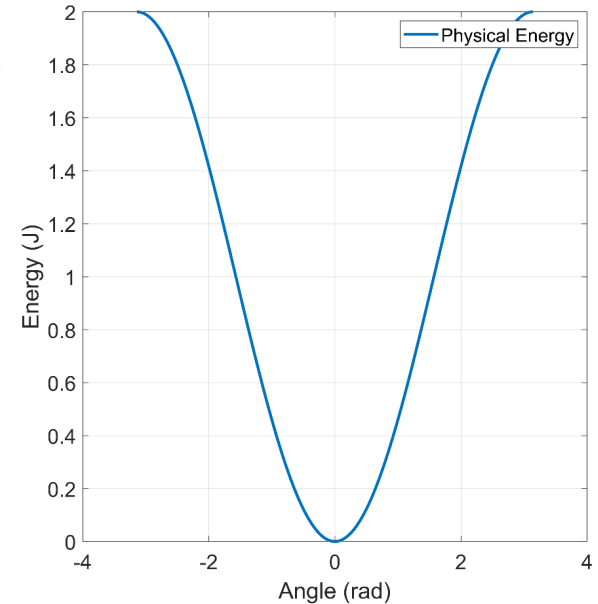
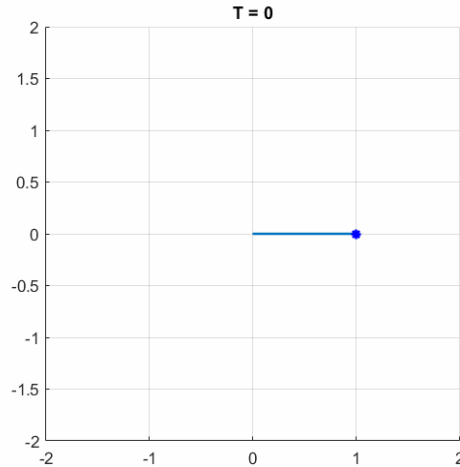
Agent Scheme

Simulation Results



# The approach

## Cooperative Passivity-Based Control



# The approach

## Cooperative Passivity-Based Control

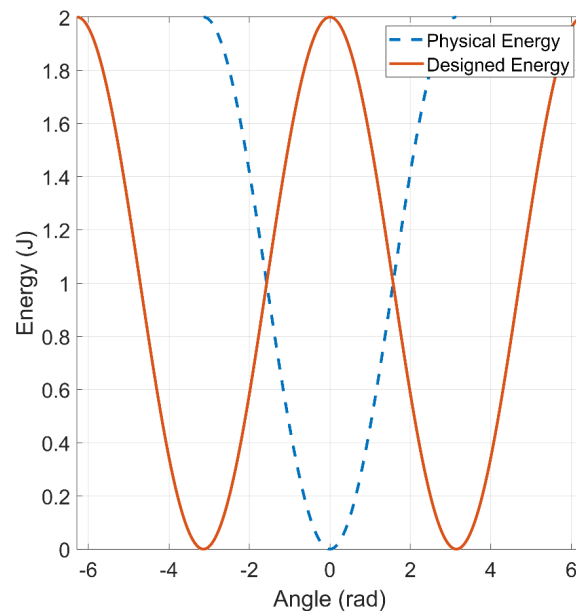
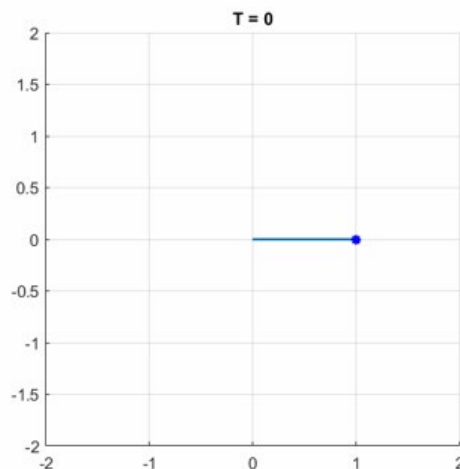
Problem Definition

IDA-PBC

Network Scheme

Agent Scheme

Simulation Results



# The approach

## Cooperative Passivity-Based Control

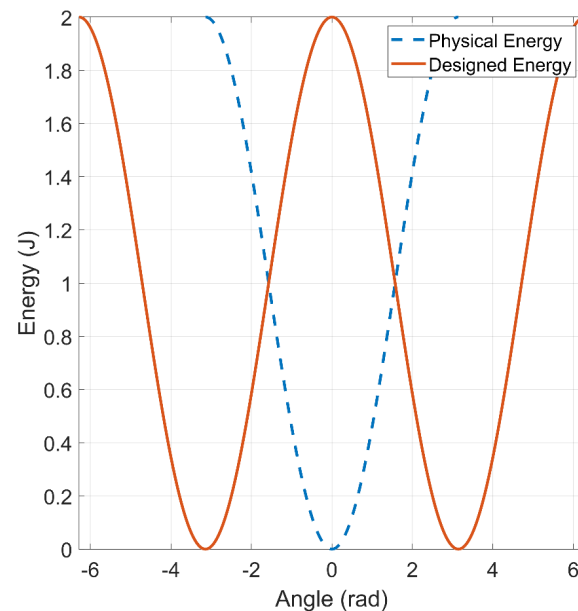
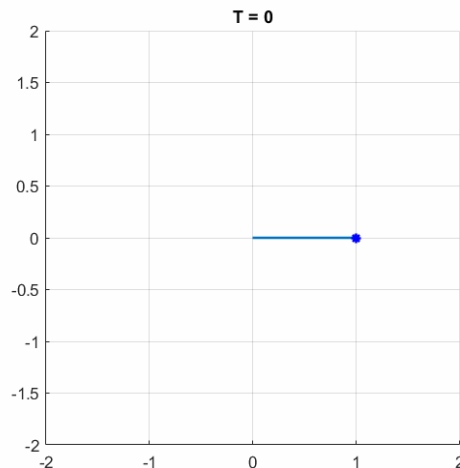
Problem Definition

IDA-PBC

Network Scheme

Agent Scheme

Simulation Results





# The approach

## Cooperative Passivity-Based Control

- Zero energy  $\rightarrow$  Control objective

Problem Definition

IDA-PBC

Network Scheme

Agent Scheme

Simulation Results



# Passivity

# Notion of Passivity

Introduction

Passivity

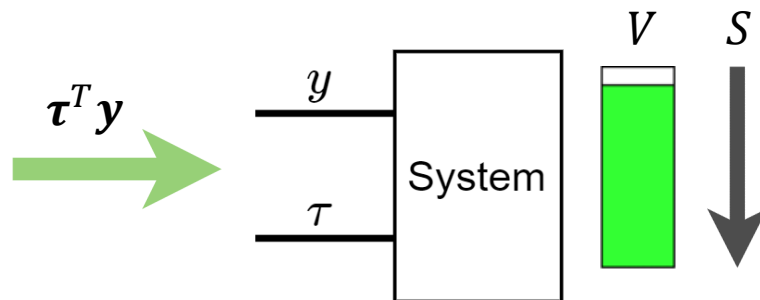
Cooperative rPBC

Experimental  
Results

Conclusions

Supplied energy is either *stored* or *dissipated*

$$\dot{V} + S = \tau^T y$$







# Cooperative Control

- No energy supply  
 $\dot{V} = -S \leq 0$  (Lyapunov)

Introduction

Passivity

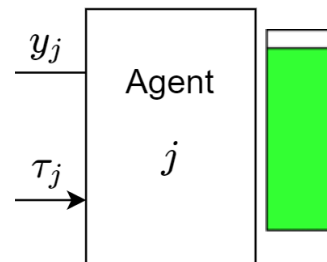
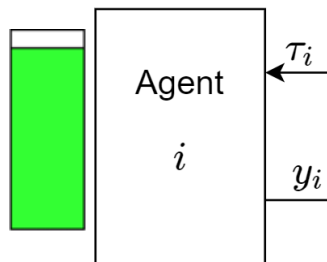
Cooperative rPBC

Experimental  
Results

Conclusions

# Cooperative Control

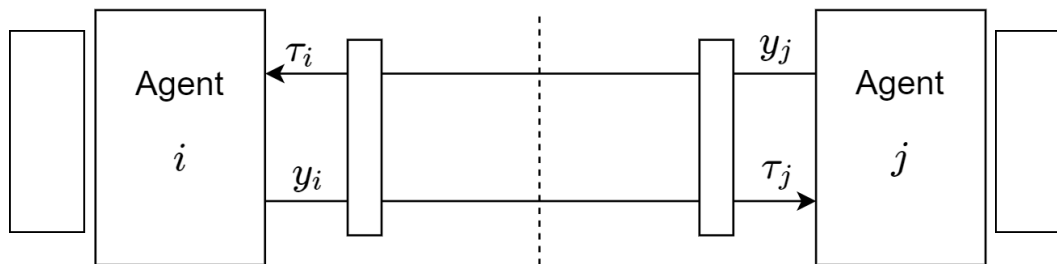
- No energy supply  
 $\dot{V} = -S \leq 0$  (Lyapunov)



# Cooperative Control

- No energy supply

$$\dot{V} = -S \leq 0 \text{ (Lyapunov)}$$





# Cooperative Control

Introduction

Passivity

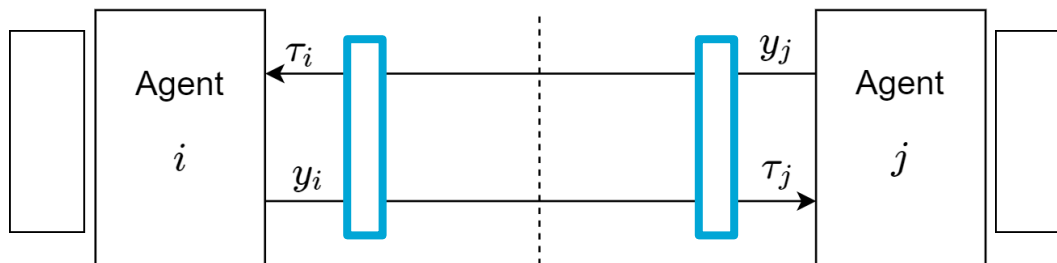
Cooperative rPBC

Experimental Results

Conclusions

- No energy supply  
 $\dot{V} = -S \leq 0$  (Lyapunov)

- Zero energy  $\rightarrow$  Cooperative control objective





# PBC with Delays

Introduction

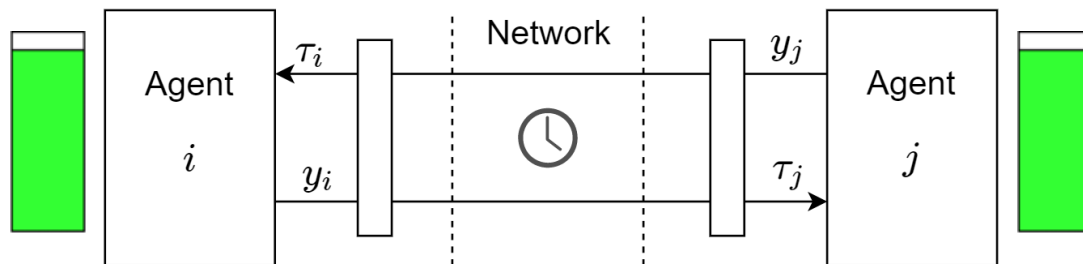
Passivity

Cooperative rPBC

Experimental Results

Conclusions

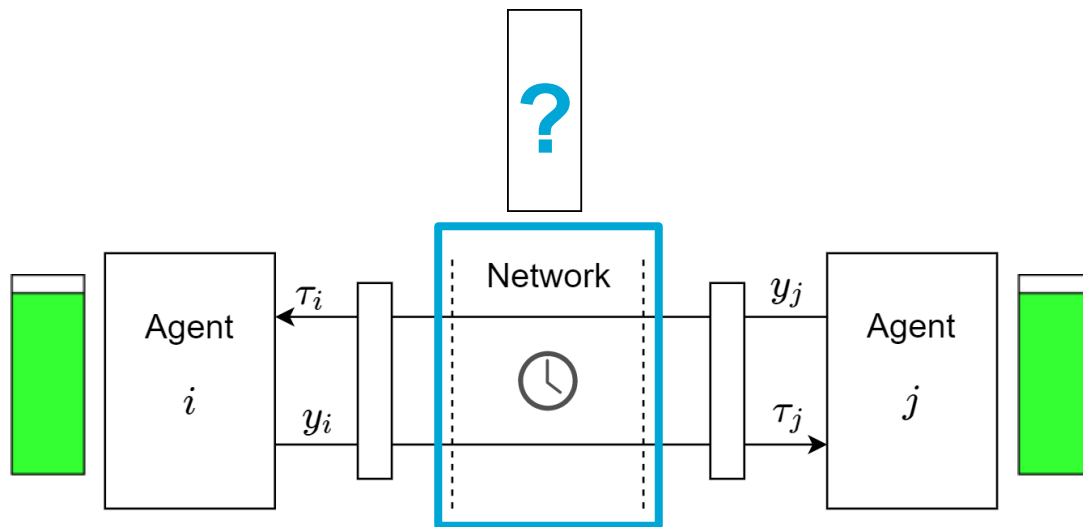
- What if delays are present?





# PBC with Delays

- No description of the energy in the network.





# PBC with Delays

Introduction

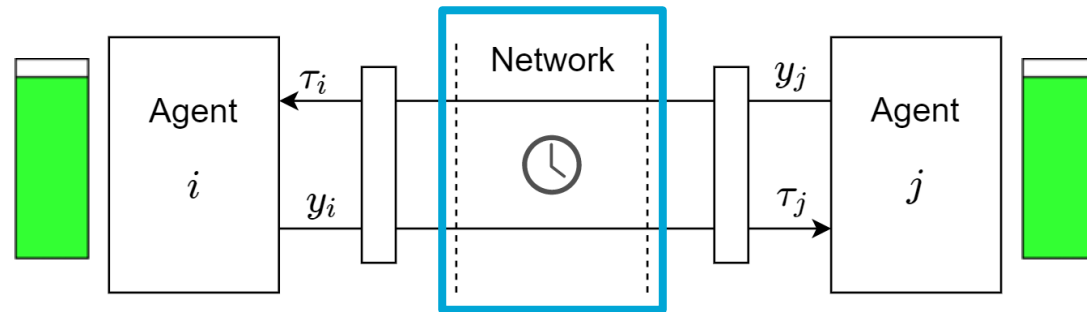
Passivity

Cooperative rPBC

Experimental Results

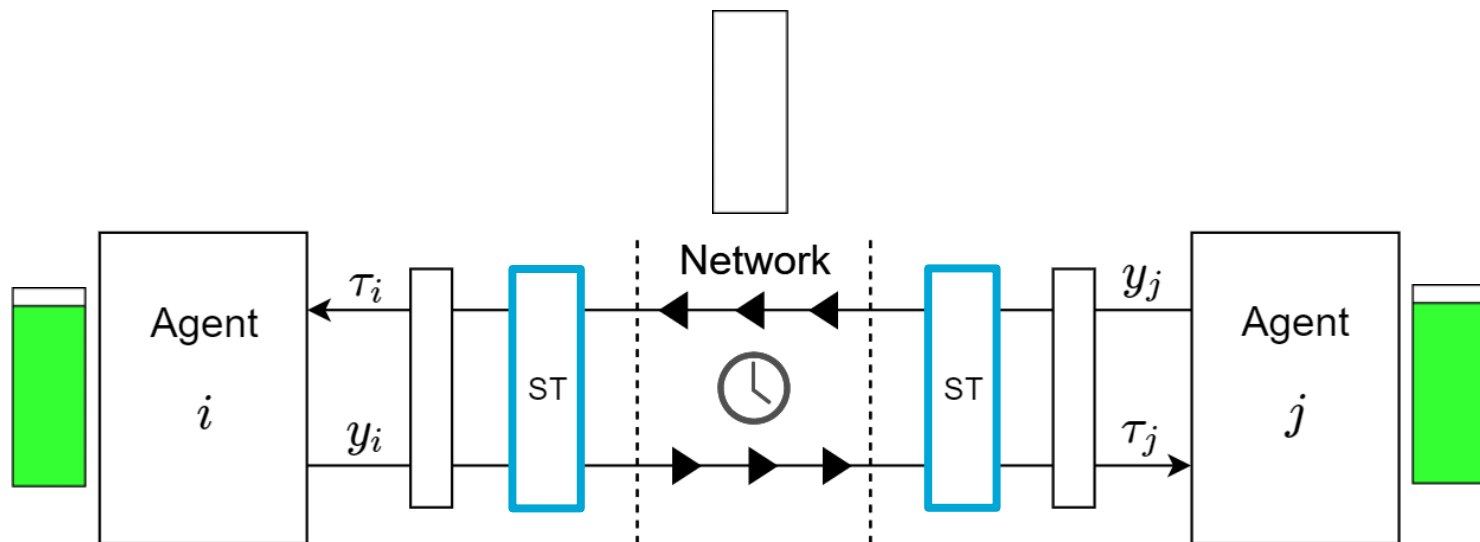
Conclusions

- No description of the energy in the network.
- **Solution:** Convert network signals to **energy packages**



# Scattering Transformation

- Convert network signals to energy packages using the Scattering Transformation (ST)

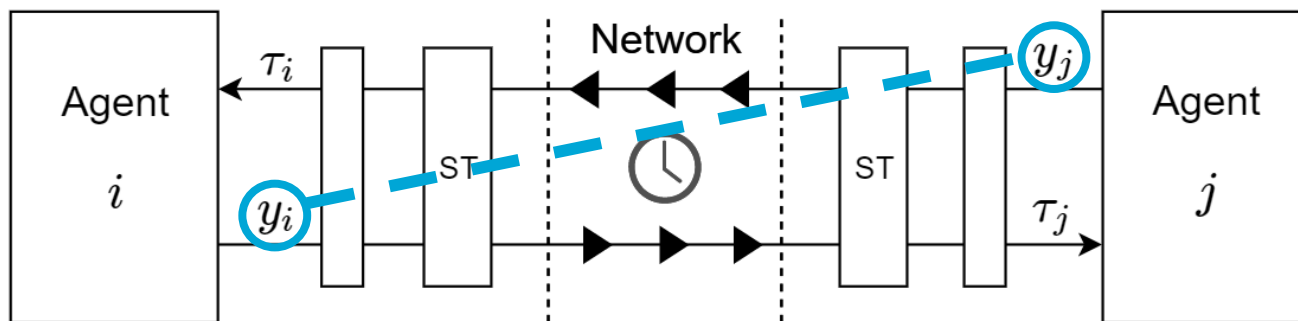




# PBC with Delays

- Output synchronization:

$$\lim_{t \rightarrow \infty} \mathbf{y}_j(t - T_{ji}) - \mathbf{y}_i = \mathbf{0}$$





# Cooperative r-Passivity-Based Control



# Output Selection

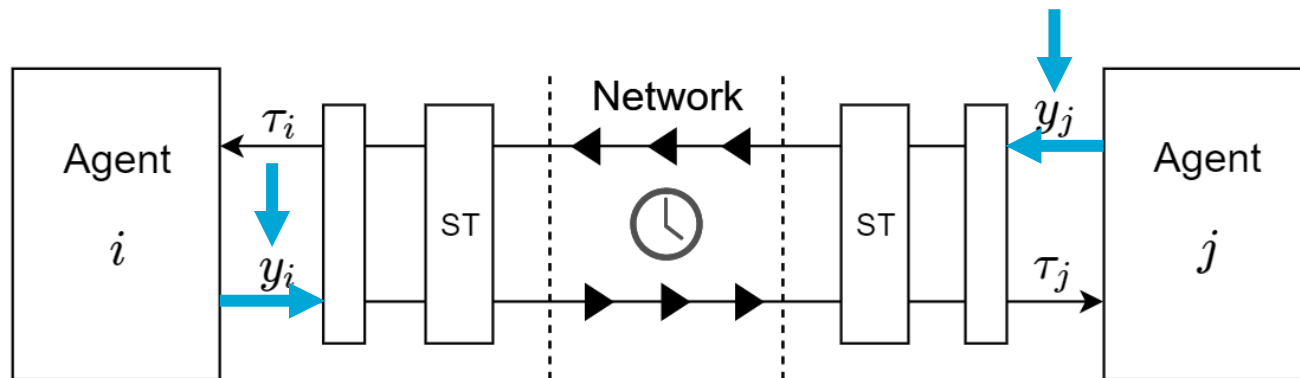
Introduction

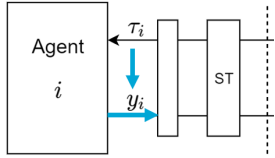
Passivity

Cooperative rPBC

Experimental Results

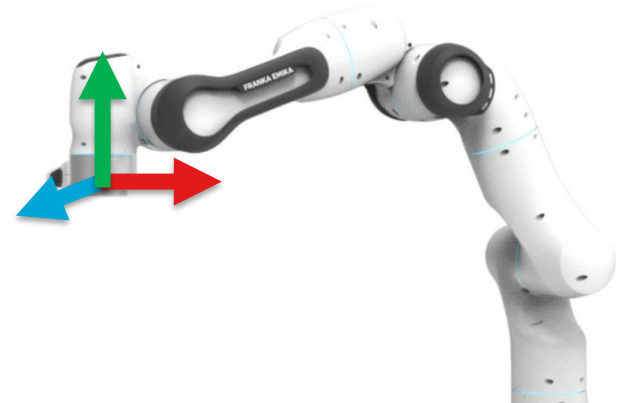
Conclusions



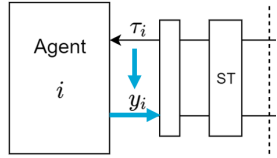


# Output Selection

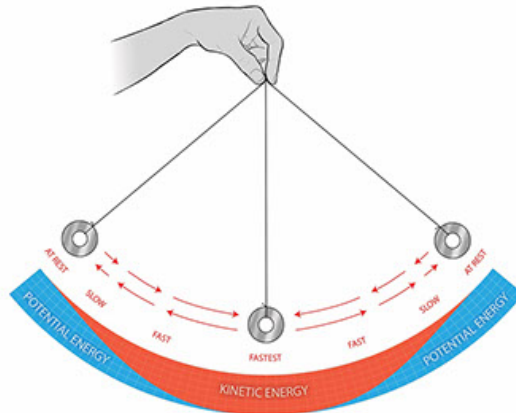
- Synchronisation of end-effector coordinates





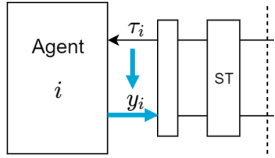
# Output Selection



- Passive outputs contain velocities



-  Potential Energy
-  Kinetic Energy



# Output Selection

- Passive outputs contain velocities

